

Maths Department

## Understanding Microstructures

CMA / Differential Equations and Numerical Analysis



Ana Ribeiro

Assistant Professor  
FCT - UNL

Post-Doc 2007/2008  
Carnegie Mellon – USA

PhD 2006  
EPFL-Switzerland

## Objectives

NATURE LOOKS FOR MINIMAL ENERGY

Find minimizers for energies in the form  $\int_{\Omega} f(\nabla u(x)) dx$ .

- $u$  may represent a deformation
- $f$  may be  $SO(3)$  invariant

## Methodology

VARIATIONAL METHODS

- Homogenization: understand macroscopic behaviour determined by the microstructure, mathematical tool :  $\Gamma$ -convergence.
- Differential Inclusions: when  $f$  is not convex.  
Example: microstructures in elastic crystals  $\nabla u(x) \in SO(3)A \cup SO(3)B$ .

## Expected Results

- Ensure existence of solutions.
- For multiple solutions problems, find a selecting principle.
- Understand the structure of sets like  $SO(3)A \cup SO(3)B$  in terms of rank one connections.

**microstructure**  
**crystals**  
**homogenization**  
**inclusion**  
**energy**  
**minima**  
**convex**  
**SO(3)**