

Mathematics Department

## H-Decompositions of Graphs



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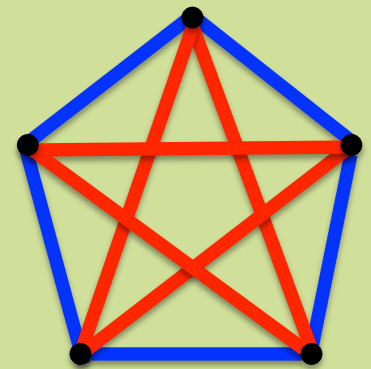
## Objectives

Given a fixed graph  $H$  we want to find the smallest number,  $f(n,H)$ , such that any graph of order  $n$  admits an  $H$ -Decomposition with at most  $f(n,H)$  elements.

In the monochromatic  $H$ -decomposition problem we want to find the smallest number,  $f(n,H,k)$ , such that any  $k$ -edge-colored graph on  $n$  vertices admits a monochromatic  $H$ -Decomposition with at most  $f(n,H,k)$  elements.

## Methodology

The  $H$ -decomposition problem is a problem in extremal graph theory. The tools used involve a wide range of methods, going from simple induction, to Szemerédi's Regularity Lemma or the Stability Method. Results known about the packing number of a graph are also widely used. Monochromatic  $H$ -Decompositions are closely related with the Ramsey Numbers.



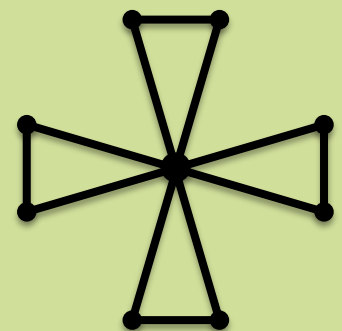
Ramsey coloring  
for  $K_3$

## Expected Results

The  $k$ -fan graph, denoted by  $F_k$ , is the graph consisting of  $k$  triangles intersecting in exactly on common vertex.

We expect to determine the function  $f(n,F_k)$ , for all  $k \geq 2$ .

For Monochromatic decompositions we expect to determine the value of the function  $f(n,K_r,k)$ , for all  $r \geq 3$  and  $k \geq 2$ , where  $K_r$  denotes the complete graph on  $r$  vertices.



4-Fan graph